

$$\mathbb{Z}^* = \{-1, +1\}$$

$$A^* = \mathbb{F}_q[T]^*$$

$$\mathbb{Z} \xleftrightarrow{\quad} q^{-1}$$

prime polynomial = monic irred $P \in \mathbb{F}_q[T]$.

"Number Theory in Function Fields"
by: M. Rosen

$$\varphi(n) = \# (\mathbb{Z}/n\mathbb{Z})^*$$

$$a^{\varphi(n)} \equiv 1 \pmod{n}$$

$$a^{p-1} \equiv 1 \pmod{p}$$

$$\begin{aligned}
 A &= \mathbb{F}_q[T] \\
 \zeta_A(s) &= \sum_{\substack{f \text{ monic} \\ f \in \mathbb{F}_q[T]}} \frac{1}{|f|^s} = \sum_{d=0}^{\infty} \sum_{\substack{f \text{ monic} \\ f \in \mathbb{F}_q[T] \\ \deg(f)=d}} \frac{1}{|f|^s} \\
 \zeta_A(s) &= \frac{1}{1-q^{1-s}} = \sum_{d=0}^{\infty} \frac{1}{q^{ds}} \sum_{\deg(f)=d} 1 \cdot t^{qs}
 \end{aligned}$$

$$\pi(x) \sim \frac{x}{\log x}$$

$$\pi_A(n) = \frac{q^n}{n} + O\left(\frac{q^{n/2}}{n}\right)$$

$$\boxed{q^n = x} = \frac{x}{\log_q(x)} + O\left(x^{1/2} \log_q(x)\right)$$

\mathbb{Z}	$\mathbb{F}_q[\Gamma]$
x	q^n
$\log x$	$\log_q q^n = \deg(f)$

$$\lim_{n \rightarrow \infty} \frac{1}{q^n} \sum_{\deg(f)=n} F(f) = \lim_{n \rightarrow \infty} \frac{1}{|q| + |q|^2 + \dots + |q|^n} \sum_{\deg(f) \leq n} F(f)$$